# Ab Initio Molecular Orbital Study on the Periodic Trends in Structures and Energies of Hypervalent Compounds: Five-Coordinated $\mathrm{XH}_{5}$ Species Containing a Group 15 Central Atom ( $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) 

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#### Abstract

An ab initio MO study employing effective core potentials (ECP) on central atoms has been carried out for a series of hypervalent $\mathrm{XH}_{5}$ hydrides, where $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi. The $\mathrm{XH}_{5}\left(D_{3 h}\right)$ and $\mathrm{XH}_{5}\left(\mathrm{C}_{4 v}\right)$ structures were found to be local minima and transition states (TSs) for Berry pseudorotation, respectively, with barriers of about $2 \mathrm{kcal} / \mathrm{mol}$. All $\mathrm{XH}_{5}\left(D_{3 k}\right)$ are thermodynamically unstable with respect to $\mathrm{XH}_{3}\left(C_{3 v}\right)+\mathrm{H}_{2}$ by over $40 \mathrm{kcal} /$ mol, and the periodic trend revealed in these stabilities is irregular. The energy decomposition analysis (EDA) was used to study the origin of this irregularity. The TSs for $\mathrm{H}_{2}$ elimination from $\mathrm{XH}_{5}\left(D_{3 h}\right)$ possessed $C_{s}$ symmetry and were equatorial-equatorial (eq-eq) for $\mathrm{X}=\mathrm{P}$, As, and Sb , whereas zwitterionic axial-equatorial (ax-eq) for $\mathrm{X}=$ Bi. The barrier heights to $\mathrm{H}_{2}$ loss are relatively high and quite similar ( $30-34 \mathrm{kcal} / \mathrm{mol}$ ) for all X , and all the $\mathrm{XH}_{5}$ species are kinetically stable. The all-electron (AE) ab initio calculation was also performed for $\mathrm{XH}_{5}\left(\mathrm{D}_{3 h}\right)$ and $\mathrm{XH}_{5}\left(C_{4 v}\right)$ with $\mathrm{X}=\mathrm{P}$, As, and Sb , showing that the effect of ECP and electron correlation on these structures was minor.


## 1. Introduction

The hypervalent or hypercoordinate compounds, an intriguing family of chemical species which break (at least seemingly) the octet rule, have attracted considerable attention in both theoretical and experimental studies. On the theoretical side, the models proposed to rationalize the nature of the "hypervalent bond" incorporated the dorbital participation in the hybridization scheme ${ }^{1}$ and, later, the formation of the three-center, fourelectron bond, ${ }^{\text {2a.b }}$ without a large contribution of $d$ atomic orbitals. ${ }^{2 c}$
The present work is a part of our $a b$ initio pseudopotential studies investigating in a systematic manner structures and energies of the closed-shell $\mathrm{XH}_{n}$ and $\mathrm{XF}_{n}$ hypervalent compounds with $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi for $n=4-7$. In the first paper ${ }^{3}$ of this series we examined the species with a coordination number $n$ equal to 4 , i.e., having formulas $\mathrm{XH}_{4}{ }^{-}$and $\mathrm{XF}_{4}{ }^{-}$. Extensive mapping of the potential energy surfaces (PES) of the four-coordinated ions ${ }^{3}$ revealed that the forms of lowest energy were those of $C_{2 v}$ symmetry, whereas their $C_{4 v}$ structures were found to be transition states (TSs) connecting $C_{2 v}$ minima in the $C_{2 v}-C_{4 v}-C_{2 v}$ pseudorotation. On the other hand, the $D_{4 h}$ forms of $\mathrm{XH}_{4}{ }^{-}$and $\mathrm{PF}_{4}{ }^{-}$appeared to be TSs for inversion of the $C_{4 v}$ structures. We also found ${ }^{3}$ that the $E\left(C_{4 v}\right)-E\left(C_{2 v}\right)$ energy differences for both $\mathrm{XH}_{4}{ }^{-}$and $\mathrm{XF}_{4}{ }^{-}$behaved irregularly

[^0]on going down the column, whereas the thermodynamic stabilities of $\mathrm{XH}_{4}^{-}\left(C_{2 v}\right)$ or $\mathrm{XF}_{4}^{-}\left(C_{2 v}\right)$ with respect to loss of $\mathrm{H}^{-}$or $\mathrm{F}^{-}$increased in the order $\mathrm{X}=\mathrm{P}<\mathrm{X}=\mathrm{As}<\mathrm{X}=\mathrm{Sb}$ $\approx \mathrm{X}=\mathrm{Bi}$. The energy decomposition analysis was used to clarify both periodic trends. ${ }^{3}$

Five-coordinated phosphorus compounds are of current theoretical and experimental interest. ${ }^{4}$ The prototype phosphorane, $\mathrm{PH}_{5}$, although not yet observed, has been one of the most extensively studied hypervalent species. The $a b$ initio calculations on $\mathrm{PH}_{5}{ }^{5-7}$ have centered on the electronic structure, equilibrium geometry, barriers to Berry and "turnstile" pseudorotation processes, and thermodynamic stability with respect to $\mathrm{PH}_{3}+\mathrm{H}_{2}$; fewer works ${ }^{5 \mathrm{~d} . e}$ have concentrated on the barrier height for the $\mathrm{H}_{2}$ elimination reaction from this species. The related $a b$ initio studies investigating substituent effects (i.e. substitution of one or more different ligands for hydrogens in the parent $\mathrm{PH}_{5}$ ) on the stabilities of the resultant phosphoranes were also reported. ${ }^{5 \text { ani. } 6.8}$ In this connection we notice the recently proposed conceptions of equatophilicity ${ }^{8}$ or equato-

[^1]riphilicity, ${ }^{6}$ demonstrating equatorial preference shown by less electronegative ligands or by ligands forming covalent bonds to phosphorus, respectively.

In contrast, almost no attention was devoted in the literature to theoretical studies of the "heavier" analogues of $\mathrm{PH}_{5}$ containing arsenic ( $\mathrm{AsH}_{5}$ ), antimony ( $\mathrm{SbH}_{5}$ ), and bismuth $\left(\mathrm{BiH}_{5}\right)$. In recent years, comparative $a b$ initio studies on molecular systems including central atoms belonging to a given main group of the periodic table have become possible through the use of pseudopotentials, which can incorporate relativistic effects. ${ }^{9}$ As ${ }^{10.11}$ in the case of $\mathrm{PH}_{5}$, there is so far no experimental evidence for the existence of $\mathrm{AsH}_{5}, \mathrm{SbH}_{5}$, or $\mathrm{BiH}_{5}$. To our knowledge, $\mathrm{AsH}_{5}$ has been the subject of one ab initio (pseudopotential) study, by Trinquier et al., ${ }^{7}$ whose contribution is also of relevance to our present work. These authors have predicted that a barrier to Berry pseudorotation of $\mathrm{AsH}_{5}$ is quite similar to that of $\mathrm{PH}_{5}$ and indicated that $\mathrm{AsH}_{5}$ is thermodynamically unstable relative to $\mathrm{AsH}_{3}+\mathrm{H}_{2}$. No vibrational analysis was done for their calculated $\mathrm{AsH}_{5}\left(D_{3 h}\right)$ and $\mathrm{AsH}_{5}\left(C_{4 v}\right)$ structures. When our paper was being revised, the results of recent $a b$ initio calculations on the series of period 6 hydrides by Schwerdtfeger et al. ${ }^{27}$ were brought to our attention. The latter authors explored relativistic effects on the geometry and thermodynamic stability of $\mathrm{BiH}_{5}$ with respect to $\mathrm{BiH}_{3}+\mathrm{H}_{2}$. We have not found in the literature any previous quantumchemical calculations on $\mathrm{SbH}_{5}$.
In this paper we report a comparative $a b$ initio pseudopotential study for the $D_{3 h}$ and $C_{4 \nu}$ structures ${ }^{22}$ of the $\mathrm{XH}_{5}$ hypervalent hydrides, where $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi . We have focused on exploring periodic trends in the (i) geometries, (ii) barriers to pseudorotation, and (iii) thermodynamic stabilities of $\mathrm{XH}_{5}$ relative to $\mathrm{XH}_{3}+\mathrm{H}_{2}$. Our concern has also been in finding the (iv) energy barriers for the $\mathrm{XH}_{5} \rightarrow \mathrm{XH}_{3}+\mathrm{H}_{2}$ decomposition reactions and, thereby, in predicting the possible existence of the $\mathrm{XH}_{5}$ species. For $\mathrm{XH}_{5}$ with $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb , the parallel all-electron (AE) $a b$ initio computations were also performed here in order to systematically study the effects of electron correlation on their structures and for the sake of comparison with the $a b$ initio pseudopotential findings.

## 2. Computational Methods

2.1. ECP Calculations. The standard effective core potentials (ECP) ${ }^{9 \mathrm{~d}}$ were used for $\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi atoms, together with the valence ( 3 s 3 p 2 d )/[3s3p2d] basis sets, ${ }^{9 \mathrm{~d} .12}$ employed and tested previously. ${ }^{3}$ For H , the polarized double- $\zeta$ (DZP) basis set of the form ( 4 s 1 p$) /\left[2 \mathrm{slp}\right.$ p was utilized. ${ }^{13}$ The structures were gradient optimized using RHF wave functions (RHF/ECP level) and, for selected cases, with the second-order Møller-Plesset

[^2]perturbation theory ${ }^{14 \mathrm{a}}$ (MP2/ECP ${ }^{15}$ level). Occasionally, UHF wave functions and the UHF based second-order Møller-Plesset perturbation theory and quadratic configuration interaction technique ${ }^{14 c}$ were employed; these theoretical levels will be referred to as UHF/ECP, UMP2/ECP, and UQCISD/ECP, respectively. The subsequent vibrational frequencies were evaluated numerically using analytical gradients. ${ }^{16.17}$ The final correlation energy was computed using Møller-Plesset perturbation theory through fourth order ${ }^{14 \mathrm{~b}}$ including triple excitations (MP4SDTQ), but hereafter denoted MP4/ECP.
2.2. AE Calculations. For $\mathrm{P}, \mathrm{As}$, and Sb atoms, the (4321/ $421),(43321 / 4321 / 31)$, and (433321/43321/421) basis sets of Huzinaga et al. ${ }^{12}$ were used, respectively, supplemented with two d polarization functions. ${ }^{12}$ For H , we employed the DZP basis described above. Geometry optimizations and subsequent frequency calculations were done using both RHF and secondorder Møller-Plesset perturbation theory ${ }^{14 \mathrm{a}}$ methods; ${ }^{16.17}$ these computational levels will be referred to as RHF/AE and MP2/ AE , respectively. The RHF/AE frequencies were computed analytically, whereas the MP2/AE frequencies were evaluated numerically using analytical gradients.

## 3. Results

3.1. RHF/ECP and MP2/ECP Structures. The $D_{3 h}$ structures of $\mathrm{XH}_{5}$ are found to be minima on the RHF/ECP potential energy surfaces (PES) (with zero imaginary frequencies) for all X (Figure 1). The axial (ax) and equatorial (eq) bond lengths increase gradually from $\mathrm{PH}_{5}\left(D_{3 h}\right)$ to $\mathrm{BiH}_{5}\left(D_{3 h}\right)$, as qualitatively expected from the respective atomic radii of the central atoms. ${ }^{23}$ However, the differences between the axial and equatorial distances, $\Delta(a x-e q)$, do not show a regular trend. At RHF/ECP, these differences are $0.059,0.073,0.066$, and $0.084 \AA$ for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi , respectively, thus revealing a smaller value than expected for $\mathrm{X}=\mathrm{Sb}$. The MP2/ECP geometry optimization of $\mathrm{XH}_{5}\left(D_{3 h}\right)$ (Figure 1), carried out mainly for the purpose of the $\mathrm{XH}_{5}\left(D_{3 h}\right) \rightarrow \mathrm{XH}_{3}+\mathrm{H}_{2}$ decomposition study discussed below, led only to minor changes in comparison with the RHF/ECP findings. Namely, for $\mathrm{X}=$ $\mathrm{P}, \mathrm{As}$, and Sb , the distances are within $0.006 \AA$, and for $\mathrm{X}=$ Bi , they agree to $0.01 \AA$. The $\Delta(\mathrm{ax}-\mathrm{eq})$ values predicted from the MP2/ECP calculation are $0.054,0.067,0.059$, and $0.072 \AA$ for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi , respectively, thus showing also a "minimum" for $\mathrm{X}=\mathrm{Sb}$.
The RHF/ECP $C_{4 v}$ structures of $\mathrm{XH}_{5}$ lie consistently higher in energy than the corresponding $D_{3 h}$ forms (Figure 1). A vibrational analysis indicates that the $C_{4 v}$ structures are saddle points (one imaginary frequency) for the Berry pseudorotation ${ }^{11}$ process (Scheme 1). As expected, the apical (ap) and basal (bas) distances in the $C_{4 v}$ structures lengthen gradually on going down the column, whereas the basal hydrogen-central atomapical hydrogen bond angles tend to widen only slightly in this

[^3]

Figure 1. $D_{3 h}$ and $C_{4 \nu}$ structures of $\mathrm{XH}_{5}(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi$)$ optimized at the RHF/ECP level (bond lengths in angstroms, bond angles in degrees). Values shown in boldface correspond to RHF energies relative to the $D_{3 h}$ structures ( $\mathrm{kcal} / \mathrm{mol}$ ); the number of associated imaginary frequencies is given in square brackets. For $D_{3 h}$ structures, the MP2/ECP geometrical parameters together with the number of corresponding imaginary frequencies are also shown (in italics).

Scheme 1. Illustration of Berry Pseudorotation for the $\mathrm{XH}_{5}$ Species ( $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) Exchanging the Axial (H1, H3) and Equatorial (H4, H5) Pairs of Ligands through the $C_{4 v}$ Transition State

direction (Figure 1). The differences between the basal and apical distances, $\Delta$ (bas-ap), are $0.055,0.067,0.065$, and 0.079 $\AA$, for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi , respectively, thus showing again a relatively small value for $\mathrm{X}=\mathrm{Sb}$.
3.2. RHF/AE and MP2/AE Structures. The $D_{3 h}$ and $C_{4 v}$ structures of $\mathrm{XH}_{5}$ as found from the RHF/AE and MP2/AE optimizations for $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb are displayed in Figure 2. A comparison of Figures 1 and 2 reveals that good agreement exists between the RHF/ECP and RHF/AE geometries. That is, for $\mathrm{X}=\mathrm{P}$ and As, the relevant distances are within $0.005 \AA$ ( $D_{3 h}$ and $C_{4 v}$ forms included), and the bond angles are within $0.2^{\circ}$; for $\mathrm{X}=\mathrm{Sb}$, the distances agree to $0.022 \AA$ and the bond angles differ by $0.2^{\circ}$. For $\mathrm{XH}_{5}\left(D_{3 h}\right)$, the MP2/ECP and MP2/ AE distances are within $0.013 \AA$. Thus, as in $\mathrm{XH}_{4}{ }^{-}$and $\mathrm{XF}_{4}{ }^{-}$ studied previously, ${ }^{3}$ we found here a good correspondence between the $a b$ initio ECP and AE structural predictions for the hypervalent species including $\mathrm{P}, \mathrm{As}$, and Sb central atoms.


Figure 2. $D_{3 h}$ and $C_{4 v}$ structures of $\mathrm{XH}_{5}(\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb$)$ optimized at the RHF/AE and MP2/AE levels (bond lengths in angstroms, bond angles in degrees). Values shown in boldface correspond to RHF energies relative to the $D_{3 h}$ structures ( $\mathrm{kcal} / \mathrm{mol}$ ); the number of associated imaginary frequencies is given in square brackets. Values in italics are from the MP2 calculation.

The MP2/AE geometry optimizations of the $D_{3 h}$ and $C_{4 v}$ forms of $\mathrm{XH}_{5}$ with $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb (Figure 2) resulted again in minor changes as compared to the RHF/AE structures: the bond lengths are within $0.009 \AA$, and the bond angles agree to within $0.4^{\circ}$. The minor correlation effects on the axial bond lengths in $\mathrm{XH}_{5}\left(D_{3 h}\right)$ indicate that these bonds have already been described adequately using the RHF wave function. This is in sharp contrast with the $\mathrm{XH}_{4}{ }^{-}$hypervalent species, having $C_{2 v}$ pseudo-trigonal-bipyramidal structures as the lowest energy structures, where the MP2 correlation effects not only reduced appreciably their axial distances but, for $\mathrm{X}=\mathrm{P}$ and As , even changed the nature of these species from unstable saddle points to stable minima. ${ }^{3}$

A further inspection of Figures 1 and 2 shows that there is a full agreement between the vibrational analysis results provided by the $a b$ initio ECP and AE methods used as far as the number of the corresponding imaginary frequencies is concerned (a complete set of the vibrational frequencies is given in the supporting information).

### 3.3. Periodic Trend in the Barriers to Berry Pseudoro-

 tation. The barrier to Berry pseudorotation of $\mathrm{PH}_{5}$ has been studied in great detail by $a b$ initio MO methods. ${ }^{5 a b e . e . g-j .6 .7 ~ T h e ~}$ $a b$ initio calculations show that the barrier height corresponding to this pseudorotation process (Scheme 1) is quite low: the SCF estimates range from about 2 to about $5 \mathrm{kcal} / \mathrm{mol}$, depending on the basis set used and the geometries assumed. Including electron correlation effects and zero-point energies (ZPE) further reduces this barrier. For instance, Schleyer and co-workers ${ }^{5 a}$ reported recently the value of $1.1 \mathrm{kcal} / \mathrm{mol}$ obtained at the MP4/ 6-31G(d) + ZPE level.The periodic trend in the barriers to Berry pseudorotation within the $\mathrm{XH}_{5}$ series ( $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) has not been studied before. As we already noticed from Figures 1 and 2 the RHF/ECP and RHF/AE barriers appeared not to be sensitive to the central atom, being about $3 \mathrm{kcal} / \mathrm{mol}$. The correlation effects at MP4/ECP reduce the barriers by $c a .1 \mathrm{kcal} / \mathrm{mol}$ for

Table 1. MP2 and MP4 Energy Barriers ${ }^{a}$ to Berry Pseudorotation for $\mathrm{XH}_{5}(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi$)$

| species | $\mathrm{MP}^{2} / \mathrm{ECP}^{b}$ | $\mathrm{MP}^{b} / \mathrm{AE}^{c}$ |
| :--- | :---: | :---: |
| $\mathrm{PH}_{5}$ | 1.9 | 2.0 |
| $\mathrm{AsH}_{5}$ | 2.1 | 2.2 |
| $\mathrm{SbH}_{5}$ | 2.3 | 2.2 |
| $\mathrm{BiH}_{5}$ | 1.9 |  |

${ }^{a}$ In kcal/mol. ${ }^{b}$ At the RHF/ECP optimized geometries. ${ }^{c}$ At the MP2/ AE optimized geometries.
Table 2. Natural Charges for the $D_{3 h}$ and $C_{4 \nu}$ Structures of $\mathrm{XH}_{5}$ ( $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) from the RHF/ECP Calculations ${ }^{a}$

| species | $Q(\mathrm{X})$ | $Q\left(\mathrm{H}_{\mathrm{ax}}\right)$ | $Q\left(\mathrm{H}_{\mathrm{eq}}\right)$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{PH}_{5}\left(D_{3 h}\right)$ | +0.750 | -0.248 | -0.084 |
| $\mathrm{AsH}_{5}\left(D_{3 h}\right)$ | +0.922 | -0.285 | -0.117 |
| $\mathrm{SbH}_{5}\left(D_{3 h}\right)$ | +1.354 | -0.352 | -0.217 |
| $\mathrm{BiH}_{5}\left(D_{3 h}\right)$ | +1.263 | -0.341 | -0.194 |
| species | $Q(\mathrm{X})$ | $Q\left(\mathrm{H}_{\mathrm{ap}}\right)$ | $Q\left(\mathrm{H}_{\mathrm{bas}}\right)$ |
| $\mathrm{PH}_{5}\left(C_{4 v}\right)$ | +0.716 | -0.034 | -0.170 |
| $\mathrm{AsH}_{5}\left(C_{4 v}\right)$ | +0.896 | -0.072 | -0.206 |
| $\mathrm{SbH}_{5}\left(C_{4 v}\right)$ | +1.342 | -0.181 | -0.290 |
| $\mathrm{BiH}_{5}\left(C_{4 v}\right)$ | +1.254 | -0.164 | -0.272 |

${ }^{a}$ Subscripts ax, eq, ap, and bas stand for axial, equatorial, apical, and basal, respectively.
all X , and the MP2/AE predictions for $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb are essentially the same as the MP4/ECP findings (Table 1). Thus, we can conclude that all $\mathrm{XH}_{5}$ are nonrigid and their Berry pseudorotation barriers are not sensitive to a change of X, being about $2 \mathrm{kcal} / \mathrm{mol}$ at our best MP4/ECP level.
3.4. RHF/ECP Natural Charges for $\mathbf{X H}_{5}\left(D_{3 h}\right)$ and $\mathbf{X H}_{5^{-}}$ ( $C_{4 v}$ ). The RHF/ECP net charges for the $D_{3 h}$ and $C_{4 v}$ structures of $\mathrm{XH}_{5}$ computed by using the natural population analysis (NPA) ${ }^{18}$ are ${ }^{19-25}$ reported in Table 2. For the $D_{3 h}\left(C_{4 v}\right)$ forms, the charge separation between the central atom X and the axial and equatorial (apical and basal) hydrogens increases on going from $\mathrm{PH}_{5}$ to $\mathrm{AsH}_{5}$ to $\mathrm{SbH}_{5}$, and it is actually slightly less for $\mathrm{BiH}_{5}$ than $\mathrm{SbH}_{5} .{ }^{26}$ The negative charges on the hydrogens in $\mathrm{XH}_{5}\left(D_{3 h}\right)$ and $\mathrm{XH}_{5}\left(C_{4 v}\right)$ fall into two groups (see Table 2). The first group includes the $\mathrm{XH}_{5}$ species with $\mathrm{X}=\mathrm{P}$ and As, where the negative charges on the axial or equatorial hydrogens in the $D_{3 h}$ forms are similar as are those on the apical or basal hydrogens in the $C_{4 v}$ forms. The same holds for the second group containing the $\mathrm{XH}_{5}$ species with $\mathrm{X}=\mathrm{Sb}$ and Bi . For the $D_{3 h}$ structures, the axial hydrogens are more negatively

[^4]Table 3. Energies of the Reactions $\mathrm{XH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{XH}_{5}(\mathrm{X}=\mathrm{P}$, $\mathrm{As}, \mathrm{Sb}$, and Bi$)^{a}$

| reaction | RHF/ECP | $\mathrm{RHF}^{b} / \mathrm{AE}^{d}$ | $\mathrm{MP}^{2} / \mathrm{ECP}^{c}$ | $\mathrm{MP}^{2} / \mathrm{AE}^{e}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{PH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{PH}_{5}$ | 44.8 | 47.6 | 45.3 | 46.7 |
| $\mathrm{AsH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{AsH}_{5}$ | 55.2 | 60.9 | 54.6 | 58.1 |
| $\mathrm{SbH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{SbH}_{5}$ | 50.0 | 45.3 | 50.2 | 44.2 |
| $\mathrm{BiH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{BiH}_{5}$ | 75.4 |  | 73.0 |  |

${ }^{a}$ In kcal/mol. ${ }^{b}$ The RHF/ECP optimized geometries of $\mathrm{XH}_{3}$ are (the first entry is the bond length, in angstroms, and the second entry is the bond angle, in degrees), for $\mathrm{PH}_{3}, 1.409$ and 95.3 , for $\mathrm{AsH}_{3}, 1.510$ and 94.5, for $\mathrm{SbH}_{3}, 1.697$ and 93.8, and, for $\mathrm{BiH}_{3}, 1.759$ and 92.5. The RHF/ECP equilibrium distance of $\mathrm{H}_{2}$ is $0.735 \AA .{ }^{c}$ At the RHF/ECP optimized geometries. ${ }^{d}$ The RHF/AE optimized geometries of $\mathrm{XH}_{3}$ are (the first entry is the bond length, in angstroms, and the second entry is the bond angle, in degrees), for $\mathrm{PH}_{3}, 1.411$ and 95.3 , for $\mathrm{AsH}_{3}, 1.510$ and 94.3, and, for $\mathrm{SbH}_{3}, 1.712$ and 94.1. ${ }^{e}$ At the MP2/AE optimized geometries. The MP2/AE optimized geometries of $\mathrm{XH}_{3}$ are (the first entry is the bond length, in angstroms, and the second entry is the bond angle, in degrees), for $\mathrm{PH}_{3}, 1.415$ and 93.6 , for $\mathrm{AsH}_{3}, 1.504$ and 92.4, and, for $\mathrm{SbH}_{3}, 1.707$ and 92.5 . The MP2/AE equilibrium distance of $\mathrm{H}_{2}$ is $0.739 \AA$.


Figure 3. Graphic representation of the $\mathrm{XH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{XH}_{5}$ reaction energies as functions of the central atom X .
charged than the equatorial ones. This is consistent with the longer (and weaker) axial bonds in comparison with the equatorial bonds. In the $C_{4 v}$ structures, the negative charge resides predominantly on the basal hydrogens, which again is in correspondence with the longer basal distances as compared to the apical distances (cf. Figures 1 and 2).
3.5. Periodic Trend in the Thermodynamic Stabilities of $\mathrm{XH}_{5}$ Relative to $\mathbf{X H}_{3}+\mathbf{H}_{2}$. It has been pointed out previously ${ }^{5 \mathrm{a},-\mathrm{e} . \mathrm{h}-\mathrm{j} .7}$ that $\mathrm{PH}_{5}\left(D_{3 h}\right)$ is thermodynamically unstable relative to $\mathrm{PH}_{3}\left(C_{3 v}\right)+\mathrm{H}_{2}$. In this context an issue of the thermodynamic stabilities of $\mathrm{AsH}_{5}\left(D_{3 h}\right), \mathrm{SbH}_{5}\left(D_{3 h}\right)$, and $\mathrm{BiH}_{5}-$ ( $D_{3 h}$ ) with respect to $\mathrm{H}_{2}$ dissociation can be addressed. In particular, a question arises: what is the periodic trend in these stabilities?

In Table 3 the RHF/ECP and MP4/ECP energies of the reactions $\mathrm{XH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{XH}_{5}$ for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi are presented; these energies are also depicted in Figure 3 as functions of X . For $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb , the corresponding RHF/ AE and MP2/AE estimates are given in Table 3 for comparison. The calculations show that, like $\mathrm{PH}_{5}$, its "heavier" $\mathrm{XH}_{5}$ analogues with $\mathrm{X}=\mathrm{As}, \mathrm{Sb}$, and Bi are thermodynamically unstable relative to $\mathrm{XH}_{3}+\mathrm{H}_{2}$, i.e., at least by over $40 \mathrm{kcal} /$ mol. One also sees that an energy difference between the $\mathrm{XH}_{5}$
and $\mathrm{XH}_{3}+\mathrm{H}_{2}$ systems is little affected by electron correlation. Interestingly, the periodic trend revealed in the $\mathrm{XH}_{5}$ stabilities with respect to $\mathrm{H}_{2}$ loss is irregular. That is, the endothermicity of the reaction $\mathrm{XH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{XH}_{5}$ increases on going from $\mathrm{X}=$ $P$ to $X=A s$, decreases on going from $X=A s$ to $X=S b$, and then increases sharply with $\mathrm{X}=\mathrm{Bi}$ (see Figure 3 or Table 3). The large endothermicity of the $\mathrm{BiH}_{3}+\mathrm{H}_{2} \rightarrow \mathrm{BiH}_{5}$ reaction of $73 \mathrm{kcal} / \mathrm{mol}$ at MP4/ECP compares favorably with the recent prediction by Schwerdtfeger et al. of $c a .79 \mathrm{kcal} / \mathrm{mol},{ }^{27}$ based ${ }^{28-33}$ on the quadratic configuration interaction (QCI) relativistic pseudopotential calculation.

Further examination of the RHF/ECP (MP4/ECP) reaction energies in Table 3 or Figure 3 suggests that the irregularity found is caused by $\mathrm{X}=\mathrm{Sb}$, whose central atom does not follow the periodic trend. We also note here that the AE calculations confirm the ECP behavior in the endothermicity in question on passing from $\mathrm{X}=\mathrm{P}$ to $\mathrm{X}=\mathrm{As}$ to $\mathrm{X}=\mathrm{Sb}$; thus, this is not an artifact of the ECP model.
3.6. Transition State Structures and Barrier Heights for $\mathbf{H}_{2}$ Elimination from $\mathbf{X H}_{5}$. The $C_{s}$ transition state (TS) structures for the $\mathrm{XH}_{5} \rightarrow \mathrm{XH}_{3}+\mathrm{H}_{2}(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi$)$ decomposition reactions located at the RHF/ECP and MP2/ECP levels are depicted in Figure 4. The RHF/ECP net charges computed at these TSs by using $\mathrm{NPA}^{18}$ are shown in Figure 5. A vibrational analysis reveals that all the structures in Figure 4 have only one imaginary frequency; thus, they are genuine transition states. The reaction coordinate vectors, corresponding to the imaginary frequencies at each computational level (Figure 6), indicate clearly the TSs found are indeed for elimination of $\mathrm{H}_{2}$ from $\mathrm{XH}_{5}\left(D_{3 h}\right)$. It is easily seen from Figures 4-6 that two kinds of transition states appear, differing significantly in both geometry and charge distribution.

The first kind involves an elimination of two equatorial (eq) hydrogens, with the $\mathrm{X}-\mathrm{H}_{\mathrm{eq}}$ bonds being broken nearly synchronously (eq-eq elimination). The TSs for the eq-eq elimination were found here for $\mathrm{X}=\mathrm{P}$ at RHF/ECP and for X $=\mathrm{P}, \mathrm{As}$, and Sb at MP2/ECP. The eq-eq TSs can be viewed as distorted $C_{2 v}$ structures in which the degree of distortion and the asymmetry of the $\mathrm{X}-\mathrm{H}_{\mathrm{eq}}$ broken bonds increase on passing from $\mathrm{X}=\mathrm{P}$ to $\mathrm{X}=\mathrm{As}$ to $\mathrm{X}=\mathrm{Sb}$, as does the $\mathrm{H}-\mathrm{H}$ distance between the departing H atoms (for the trend see the MP2/ECP results in Figure 4). The calculated natural charges (Figure 5) indicate that the eq-eq TSs are only moderately polarized, especially for $\mathrm{X}=\mathrm{P}$ and As. In particular, the H atoms of the forming $\mathrm{H}_{2}$ product in these structures bear charges which are close to zero.
(27) Schwerdtfeger, P.: Heath, G. A.; Dolg. M.: Bennett, M. J. Am. Chem. Soc. 1992, 114, 7518. The cited energies were estimated from Figure 7 of this work.
(28) The barriers were estimated on the basis of the MP4/ECP energies taken from Tables 3 and 4.
(29) The latter type of selection of the $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$ subsystems was suggested by reviewers.
(30) These authors arrived at the TS having $C_{2 v}$ symmetry; however, it was shown later (ref 5 d ) that the $C_{2 v}$ TS had two imaginary frequencies.
(31) This was confirmed in the calculations by Reed and Schleyer (ref 5d).
(32) It was suggested (ref 5e) that in the presence of catalytic amounts of acids the barrier for $\mathrm{H}_{2}$ abstraction from $\mathrm{PH}_{5}$ might be decreased significantly.
(33) As previously, ${ }^{3}$ one may expect that some of the trends discussed in the present work are influenced by the relativistic contributions from the "heavy" species. ${ }^{9 \mathrm{~d}}$ In order to examine computationally the influence of relativistic effects on a given molecular property, it is necessary to compare results of relativistic and nonrelativistic calculations on that property. In fact, Schwerdtfeger et al. found on the basis of the QCI pseudopotential calculations that the relativistic effects substantially decreased the thermodynamic stability of $\mathrm{BiH}_{5}$ relative to $\mathrm{BiH}_{3}+\mathrm{H}_{2}$, i.e., by ca. $35 \mathrm{kcal} / \mathrm{mol}$. ${ }^{27}$


Figure 4. Optimized $\mathrm{C}_{\mathrm{s}}$ transition state structures for $\mathrm{H}_{2}$ elimination from $\mathrm{XH}_{5}\left(D_{3 h}\right)(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi$)$ (bond lengths in angstroms, bond angles in degrees). The number of associated imaginary frequencies is given in square brackets followed by the corresponding imaginary frequencies $\left(\mathrm{cm}^{-1}\right)$. Results are from the RHF/ECP and MP2/ECP calculations unless specified otherwise. Values in parentheses for $\mathrm{X}=$ Sb and Bi are from the UHF/ECP calculation, whereas those in curly brackets for $\mathrm{X}=\mathrm{Bi}$ were obtained at the UQCISD/ECP level.

The TSs of the second kind arise from the elimination of axial ( ax ) and equatorial hydrogens ( $\mathrm{ax}-\mathrm{eq}$ elimination). The transition state structures corresponding to the ax-eq elimination were found for $\mathrm{X}=\mathrm{As}, \mathrm{Sb}$, and Bi at RHF/ECP and for $\mathrm{X}=$ Bi at MP2/ECP (Figure 4). NPA carried out at the ax-eq TSs reveals that there is a large charge separation between one of the (axial) H atoms of the forming $\mathrm{H}_{2}$ and the remaining $\mathrm{XH}_{4}$ fragment (Figure 5). Thus, the TSs for the ax -eq elimination can be described as having zwitterionic $\mathrm{XH}_{4}{ }^{+} \cdots \mathrm{H}^{-}$nature. The salient structural features of the ionic TSs are (i) a very long axial $\mathrm{X}-\mathrm{H}$ distance involving the departing hydrogen, which increases on going from $\mathrm{X}=\mathrm{As}$ to $\mathrm{X}=\mathrm{Sb}$ to $\mathrm{X}=\mathrm{Bi}$, and (ii) a relatively long $\mathrm{H}-\mathrm{H}$ distance of the forming $\mathrm{H}_{2}$, increasing again in the same direction (for the trends see the RHF/ECP results in Figure 4). We stress here that when the geometry was optimized at the correlated MP2/ECP level, for $\mathrm{X}=\mathrm{As}$ and Sb , the ax-eq zwitterionic TSs collapsed to the eq-eq ones. On the other hand, our MP2/ECP searches for the eq-eq TS with $\mathrm{X}=\mathrm{Bi}$ resulted invariably in the ax-eq ionic structure. As a result, at the higher level of theory, the TSs predicted here for $\mathrm{H}_{2}$ elimination from $\mathrm{XH}_{5}\left(D_{3 h}\right)$ are of the eq-eq type for all X except for $\mathrm{X}=\mathrm{Bi}$ (see also below).

A possible explanation of the eq-eq TSs emerges in terms of Woodward-Hoffmann rules. ${ }^{34 a}$ By the same token, for the $\mathrm{ax}-\mathrm{eq}$ TSs, the stability of the RHF wave functions should be tested. ${ }^{34 \mathrm{~b}}$ As a matter of fact, the triplet instability of the RHF/ ECP solutions for the ax-eq TSs with $\mathrm{X}=\mathrm{Sb}$ and Bi was detected here, indicating an existence of the lower energy singlet UHF wave functions for these TSs. ${ }^{35}$ Consequently, ${ }^{36}$ both TSs


Figure 5. RHF/ECP net charges at the RHF/ECP and MP2/ECP transition states for $\mathrm{H}_{2}$ elimination from $\mathrm{XH}_{5}\left(D_{3 h}\right)(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) obtained by using the natural population analysis (NPA). The symbol // means at the geometry of.
were recalculated at the UHF/ECP level, as shown in Figure 4. ${ }^{37 \text { a }}$ The noticeable structural difference between the RHF/ ECP and UHF/ECP predictions is the larger $\mathrm{H}-\mathrm{H}$ distance of the forming $\mathrm{H}_{2}$ in the latter case, especially for $\mathrm{X}=\mathrm{Bi}$ (Figure 4). ${ }^{38}$ On the other hand, the concomitant decrease in energy for these TSs is only 0.1 and $1.1 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{X}=\mathrm{Sb}$ and Bi , respectively (see below). Furthermore, the UMP2/ECP wave functions were used for recalculating the TSs with $\mathrm{X}=\mathrm{Sb}$ and Bi , which merely reproduced the RMP2/ECP results. Since the TS for $\mathrm{X}=\mathrm{Bi}$ appeared to be unique among those calculated here, it was important to check this finding at the theoretical level providing a better description of electron correlation than MP2. The UQCISD/ECP wave function was utilized for this purpose, and the resulting TS was also included in Figure 4. ${ }^{37 \mathrm{~b}}$ It is seen that, again, the ax-eq type TS was obtained. Moreover, the transition state structures computed for $\mathrm{X}=\mathrm{Bi}$ at the MP2/ECP and UQCISD/ECP levels are very similar.

[^5]

Figure 6. Reaction coordinate vector at the RHF/ECP and MP2/ECP transition states for $\mathrm{H}_{2}$ elimination from $\mathrm{XH}_{5}\left(D_{3 h}\right)(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and $\mathrm{Bi})$. The reaction coordinate vector, i.e., the direction of the normal coordinate corresponding to the imaginary frequency, was calculated at each computational level. The view of structures here is slightly different from that in Figures 4 and 5 for a clearer representation of the vector.

To account for the different nature of the TS for $\mathrm{X}=\mathrm{Bi}$ as compared to those with $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb found at the correlated level, we recall the results of section 3.5. Namely, the reverse of the reaction $\mathrm{XH}_{5} \rightarrow \mathrm{XH}_{3}+\mathrm{H}_{2}$ with $\mathrm{X}=\mathrm{Bi}$ was indicated to be the most endothermic ( $73 \mathrm{kcal} / \mathrm{mol}$, Table 3). Thus, one can expect an "early" TS for the highly exothermic $\mathrm{BiH}_{5} \rightarrow \mathrm{BiH}_{3}+\mathrm{H}_{2}$ decomposition reaction. ${ }^{20}$ Indeed, the $\mathrm{ax}-$ eq TS structures resemble much more those of the $\mathrm{XH}_{5}\left(D_{3 h}\right)$ reactants in comparison with the eq-eq TS structures (cf. Figures 1 and 4). On passing, we note that both eq-eq and ax-eq types of transition states were reported recently for $\mathrm{H}_{2}$ detachment from the $\mathrm{MH}_{4}(\mathrm{M}=\mathrm{S}, \mathrm{Se}$, and Te$)$ hypervalent species (see ref 24 for details).

Among the $\mathrm{XH}_{5} \rightarrow \mathrm{XH}_{3}+\mathrm{H}_{2}$ decomposition pathways considered, only that with $\mathrm{X}=\mathrm{P}$ was studied before. ${ }^{\text {Sd,e }}$ Kutzelnigg and Wasilewski, ${ }^{5 \mathrm{e}}$ who extensively investigated the pathway under $C_{s}$ symmetry, first pointed out the existence of the concerted ${ }^{30}$ and zwitterionic transition states at the SCF level, and found that the potential energy surface between the two TSs was very flat. They also obtained very similar barrier heights for $\mathrm{H}_{2}$ elimination from $\mathrm{PH}_{5}$ corresponding to both transition states. ${ }^{31}$ Interestingly, Kutzelnigg and Wasilewski observed that the zwitterionic TS disappeared when the correlated method was used for geometry optimization ${ }^{5 e}$ (recall the similar behavior seen above for the TSs with $\mathrm{X}=\mathrm{As}$ and Sb ). Here, at the RHF/ECP level, we have reported only an eq-eq "concerted" TS for $\mathrm{X}=\mathrm{P}$. The relevant geometry (Figure 4) compares favorably with the RHF/6-31G(d) one obtained earlier by employing gradient optimization methods, ${ }^{5 \mathrm{~d}}$ and it changes somewhat at MP2/ECP (but we did not search for the ax-eq ionic TS for $\mathrm{X}=\mathrm{P}$ at the RHF/ECP level).

Table 4. Barrier Heights for the $\mathrm{H}_{2}$ Elimination Reactions from $\mathrm{XH}_{5}\left(D_{3 h}\right)(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb} \text {, and } \mathrm{Bi})^{a}$

| reaction | RHF/ECP | MP2/ECP $^{c}$ | MP4/ECP $^{\text {c,d }}$ |
| :--- | :--- | :---: | :--- |
| $\mathrm{PH}_{5} \rightarrow \mathrm{PH}_{3}+\mathrm{H}_{2}$ | 45.5 | 32.6 | $32.6(30.2)$ |
| $\mathrm{AsH}_{5} \rightarrow \mathrm{AsH}_{3}+\mathrm{H}_{2}$ | $42.8^{b}$ | 33.3 | $32.9(30.9)$ |
| $\mathrm{SbH}_{5} \rightarrow \mathrm{SbH}_{3}+\mathrm{H}_{2}$ | $47.9,^{b} 47.8^{b, e}$ | 38.1 | $36.8(34.9)$ |
| $\mathrm{BiH}_{5} \rightarrow \mathrm{BiH}_{3}+\mathrm{H}_{2}$ | $38.5,^{b} 37.4^{4^{b, e}}$ | $34.0^{b}$ | $33.5^{b}(31.5)^{b}$ |

[^6]Chart 1. $\mathrm{XH}_{5}\left(D_{3 h}\right)(\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) Represented by the $\mathrm{XH}_{3}\left(D_{3 h}\right) \cdot \cdot \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{ax}}$ and the $\mathrm{XH}_{3}\left(C_{s}\right) \cdots \cdot \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{eq}}$ Interacting Subsystems (Subscripts eq and ax Denote Equatorial and Axial, Respectively)


The barrier heights for $\mathrm{H}_{2}$ elimination reactions from $\mathrm{XH}_{5}\left(D_{3 h}\right)$ ( $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi ) predicted at several computational levels are summarized in Table 4. All the energies in Table 4 are relative to the $\mathrm{XH}_{5}\left(D_{3 h}\right)$ reactants. The RHF/ECP, UHF/ECP, and MP2/ECP energies refer to the transition state structures located at each computational level, whereas the MP4/ECP values were computed assuming the MP2/ECP structures. It is seen that, for $\mathrm{X}=\mathrm{P}$, As, and Sb , the MP2/ECP energy barriers, referring to the eq-eq TSs, are substantially lower, i.e., by $9.5-$ $12.9 \mathrm{kcal} / \mathrm{mol}$, than the RHF/ECP values. For the reaction with $\mathrm{X}=\mathrm{Bi}$, having the ax -eq ionic TS, the MP2/ECP barrier drops only by 4.5 (3.4) $\mathrm{kcal} / \mathrm{mol}$ with respect to the RHF/ECP (UHF/ $E C P$ ) finding. On the other hand, all the barriers hardly decrease from MP2/ECP to MP4/ECP. The zero-point energy (ZPE) correction calculated at the MP2/ECP level lowers the barrier heights by $1.9-2.4 \mathrm{kcal} / \mathrm{mol}$. Our best MP4/ECP + ZPE barriers are still relatively high and quite similar for all X , being $30.2,30.9,34.9$, and $31.5 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi , respectively. Finally, we notice that, for the eq-eq $\mathrm{H}_{2}$ elimination from $\mathrm{PH}_{5}$, our activation barrier of $30.2 \mathrm{kcal} / \mathrm{mol}$ agrees well with the correlated (and ZPE corrected) results of earlier calculations of $31.1^{5 \mathrm{~d}}$ and $33.6^{5 \mathrm{e}} \mathrm{kcal} / \mathrm{mol}$ (the latter value has been obtained by correcting the original estimate of $36 \mathrm{kcal} /$ $\mathrm{mol}^{5 \mathrm{e}}$ for ZPE values given in footnote $d$ in Table 4).

## 4. Discussion

In order to shed more light on the irregularity found in the trend of the thermodynamic stabilities of $\mathrm{XH}_{5}$ with respect to $\mathrm{XH}_{3}+\mathrm{H}_{2}$ (section 3.5), an energy decomposition analysis (EDA) ${ }^{10}$ was applied at RHF/ECP. ${ }^{15}$ The molecular system, "supermolecule", is considered in the EDA method as composed of two interacting subsystems. Here, $\mathrm{XH}_{5}\left(D_{3 h}\right)$ were considered as composed of the $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$ "subsystems". Two different selections of the supermolecules were taken into account (Chart 1): (i) $\mathrm{XH}_{3}\left(D_{3 h}\right) \cdots{ }^{\cdot} \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{ax}}$, with the axial hydrogens forming the $\mathrm{H}_{2}$ subsystem, and (ii) $\mathrm{XH}_{3}\left(C_{s}\right) \cdots \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{eq}}$, where the $\mathrm{H}_{2}$ subsystem was represented by the axial and equatorial hydrogens. ${ }^{29}$

In the EDA scheme, ${ }^{10}$ the binding energy, $\Delta E$, the energy difference between $\mathrm{XH}_{5}$ and isolated $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$, is divided into two parts, the deformation energy, DEF, and the interaction energy, INT:

$$
\begin{aligned}
& \Delta E=E\left(\mathrm{XH}_{5}\right)-\left[E\left(\mathrm{XH}_{3}, \text { equilibrium }\right)+\right. \\
& \left.E\left(\mathrm{H}_{2}, \text { equilibrium }\right)\right]=\mathrm{DEF}+\mathrm{INT}
\end{aligned}
$$

DEF is the energy needed to distort both $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$ from their equilibrium geometries ${ }^{25}$ to the geometries they take in the $\mathrm{XH}_{5}\left(D_{3 h}\right)$ species:

$$
\begin{aligned}
& \mathrm{DEF}=\left[E\left(\mathrm{XH}_{3}, \text { distorted }\right)-E\left(\mathrm{XH}_{3}, \text { equilibrium }\right)\right]+ \\
& {\left[E\left(\mathrm{H}_{2}, \text { distorted }\right)-E\left(\mathrm{H}_{2}, \text { equilibrium }\right)\right]}
\end{aligned}
$$

INT is the energy which comes from the interaction of the distorted $\mathrm{XH}_{3}$ with distorted $\mathrm{H}_{2}$ :
$\mathrm{INT}=E\left(\mathrm{XH}_{5}\right)-\left[E\left(\mathrm{XH}_{3}\right.\right.$, distorted $)+E\left(\mathrm{H}_{2}\right.$, distorted $\left.)\right]$
The INT energy can be decomposed into five terms:

$$
\begin{aligned}
\mathrm{INT}=\mathrm{ES}+\mathrm{EX}+\operatorname{CTPLX}\left(\mathrm{H}_{2} \rightarrow\right. & \left.\mathrm{XH}_{3}\right)+ \\
& \mathrm{CTPLX}\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)+R
\end{aligned}
$$

where ES is the electrostatic interaction, EX the exchange repulsion, CTPLX $\left(\mathrm{H}_{2} \rightarrow \mathrm{XH}_{3}\right)$ the donative interaction from $\mathrm{H}_{2}$ to $\mathrm{XH}_{3}, \mathrm{CTPLX}\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)$ the back-donative interaction from $\mathrm{XH}_{3}$ to $\mathrm{H}_{2}$, and $R$ the leftover term.

Tables 5 and 6 summarize EDA results for the $\mathrm{XH}_{5}\left(D_{3 h}\right)$ series obtained assuming the $\mathrm{XH}_{3}\left(D_{3 h}\right) \cdots \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{ax}}$ and $\mathrm{XH}_{3}\left(C_{s}\right) \cdots \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\text {eq }}$ supermolecules, respectively. The energies presented in the left half of both tables were computed at the RHF/ECP geometries and will be discussed first. It is seen that, for all X, the DEF repulsion energies are not counterbalanced by the corresponding INT attraction energies, which leads to the positive, i.e., repulsive, binding energies $\Delta E$. Our purpose now is to reveal the INT energy component(s) responsible for the "extra stability" of $\mathrm{SbH}_{5}$ over $\mathrm{AsH}_{5}$, resulting in the irregularity discussed. According to the left half of Table 5, there are two factors responsible for this extra stability: (i) the much smaller exchange repulsive EX term for $\mathrm{SbH}_{5}$ as compared to $\mathrm{AsH}_{5}$ and (ii) the larger (more negative) back-donative interaction from $\mathrm{XH}_{3}$ to $\mathrm{H}_{2}, \operatorname{CTPLX}\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)$, for $\mathrm{X}=\mathrm{Sb}$ than $\mathrm{X}=\mathrm{As}$. On the other hand, results of the analysis of the $\mathrm{XH}_{3}\left(C_{s}\right) \cdots \cdot \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\text {eq }}$ supermolecules are obscure (see left half of Table 6). That is, the absolute values of all INT components, except for ES, are large and decrease monotonically down a group. For EX and both CTPLX terms, this behavior seems to follow the increase in the distances separating $\mathrm{XH}_{3}\left(C_{s}\right)$ and $\mathrm{H}_{\mathrm{ax}}-$ $\mathrm{H}_{\mathrm{eq}}$ subsystems with increasing atomic radius of X (cf. Chart 1).

In order to make a fair comparison of INT components for $\mathrm{XH}_{5}$ containing different X , especially for the $\mathrm{XH}_{3}\left(C_{5}\right) \cdots{ }^{2}-$ $\mathrm{H}_{\text {eq }}$ supermolecules, we set the EX (repulsive) term approximately constant for all X (i.e., matching the EX of $\mathrm{BiH}_{5}$ ). ${ }^{3}$ This was achieved by adjusting either the $\mathrm{X}-\mathrm{H}_{\mathrm{ax}}$ distance in $\mathrm{XH}_{3}\left(D_{3 h}\right) \cdots \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{ax}}$ (Chart 1) or the $\mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{eq}}$ distance in $\mathrm{XH}_{3}\left(C_{s}\right) \cdot \cdots \cdot \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{eq}}$ (while keeping the ratio $\mathrm{X}-\mathrm{H}_{\mathrm{ax}}$ distance/ $\mathrm{X}-\mathrm{H}_{\mathrm{eq}}$ distance constant, Chart 1). The results of the analysis of such "equal X points"-included in the right side of Tables 5 and 6-indicate consistently that the CTPLX $\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)$ term is again more stabilizing for $X=\mathrm{Sb}$ than $\mathrm{X}=\mathrm{As}$, and thus contributes to the irregularity in question. Additional support for this interpretation comes from a comparison of the ionization potentials (IPs) of both the $\mathrm{XH}_{3}\left(D_{3 h}\right)$ and $\mathrm{XH}_{3}\left(C_{s}\right)$ subsystems,

Table 5. Energy Components for the Interaction between $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$ within the $\mathrm{XH}_{5}\left(D_{3 h}\right)$ Species Assuming the $\mathrm{XH}_{3}\left(D_{3 h}\right) \cdot \cdots \cdot \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{ax}}$ Supermolecule ${ }^{a}$

|  | $D_{3 h}{ }^{\text {b }}$ |  |  |  | $D_{3 h^{\text {c }}}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{PH}_{5}$ | $\mathrm{AsH}_{5}$ | $\mathrm{SbH}_{5}$ | $\mathrm{BiH}_{5}$ | $\mathrm{PH}_{5}$ | $\mathrm{AsH}_{5}$ | $\mathrm{SbH}_{5}$ | $\mathrm{BiH}_{5}$ |
| $\Delta E$ | 44.8 | 55.2 | 50.0 | 75.4 | 64.4 | 63.1 | 50.0 | 75.4 |
| DEF | 240.6 | 254.5 | 271.4 | 291.0 | 261.0 | 265.9 | 271.1 | 291.0 |
| INT | -195.8 | -199.3 | -221.5 | -215.6 | -196.6 | -202.8 | -221.1 | -215.6 |
| ES | -57.9 | -50.1 | -42.0 | -47.6 | -57.7 | -54.5 | -41.5 | -47.6 |
| EX | 144.5 | 99.6 | 38.9 | 40.6 | 40.4 | 40.4 | 40.6 | 40.6 |
| CTPLX $\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)$ | -129.7 | -124.5 | -129.4 | -125.7 | -102.6 | -109.1 | -130.0 | -125.7 |
| $\operatorname{CTPLX}\left(\mathrm{H}_{2} \rightarrow \mathrm{XH}_{3}\right)$ | -160.9 | -123.5 | -79.4 | -68.5 | -74.0 | -74.9 | -80.7 | -68.5 |
| $R$ | 8.2 | -0.8 | -9.5 | -14.4 | -2.7 | -4.7 | -9.4 | -14.4 |

[^7]Table 6. Energy Components for the Interaction between $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$ within the $\mathrm{XH}_{5}\left(D_{3 h}\right)$ Species Assuming the $\mathrm{XH}_{3}\left(\mathrm{C}_{5}\right) \cdot \cdots \mathrm{H}_{\mathrm{ax}}-\mathrm{H}_{\mathrm{eq}}$ Supermolecule ${ }^{a}$

|  | $D_{3 h}{ }^{\text {b }}$ |  |  |  | $D_{3 h^{\text {c }}}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{PH}_{5}$ | $\mathrm{AsH}_{5}$ | $\mathrm{SbH}_{5}$ | $\mathrm{BiH}_{5}$ | $\mathrm{PH}_{5}$ | $\mathrm{AsH}_{5}$ | $\mathrm{SbH}_{5}$ | $\mathrm{BiH}_{5}$ |
| $\Delta E$ | 44.8 | 55.2 | 50.0 | 75.4 | 84.3 | 74.3 | 53.8 | 75.4 |
| DEF | 154.3 | 166.8 | 184.0 | 190.1 | 207.0 | 197.1 | 193.4 | 190.1 |
| INT | -109.5 | -111.6 | -134.0 | -114.7 | -122.7 | -122.8 | -139.6 | -114.7 |
| ES | -28.4 | -25.3 | -26.4 | -33.6 | -40.3 | -34.6 | -30.4 | -33.6 |
| EX | 585.6 | 503.4 | 406.2 | 341.7 | 338.1 | 340.9 | 343.4 | 341.7 |
| CTPLX $\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)$ | -577.8 | -518.4 | -460.4 | -373.4 | -335.0 | -356.9 | -397.7 | -373.4 |
| CTPLX $\left(\mathrm{H}_{2} \rightarrow \mathrm{XH}_{3}\right)$ | -537.8 | -455.8 | -362.3 | -262.3 | -289.1 | -297.3 | -304.1 | -262.3 |
| $\mathrm{R}$ | 448.9 | 384.6 | 308.9 | 212.9 | 203.6 | 225.2 | 249.1 | 212.9 |

${ }^{a}$ See Chart 1. RHF/ECP energies ( $\mathrm{kcal} / \mathrm{mol}$ ) calculated at the RHF/ECP geometries (subscripts ax and eq denote axial and equatorial, respectively). A negative (positive) sign indicates stabilization (destabilization). ${ }^{b}$ Within the optimized geometries (cf. Figure 1 ). ${ }^{c}$ The data after setting the EX term approximately constant (see the text).
calculated from Koopmans' theorem (KT). For $\mathrm{XH}_{3}\left(D_{3 h}\right)$, the KT IPs are $8.0,7.7,7.0$, and 6.7 eV for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi , respectively; the relevant values for $\mathrm{XH}_{3}\left(C_{s}\right)$, put in the same order, are $9.9,9.6,9.0$, and 9.1 eV . Thus, in both cases, the much lower IP for the subsystem with $\mathrm{X}=\mathrm{Sb}$ than that for X $=$ As (by $0.6-0.7 \mathrm{eV}$ ) makes charge transfer easier for the former central atom.

## 5. Conclusion

The $\mathrm{XH}_{5}\left(D_{3 h}\right)$ and $\mathrm{XH}_{5}\left(C_{4 \nu}\right)$ structures were found to be local minima and transition states for Berry pseudorotation, respectively, the corresponding pseudorotation barriers being about 2 $\mathrm{kcal} / \mathrm{mol}$. All $\mathrm{XH}_{5}\left(D_{3 h}\right)$ appeared to be thermodynamically unstable with respect to $\mathrm{XH}_{3}\left(\mathrm{C}_{3 \nu}\right)+\mathrm{H}_{2}$, and the periodic trend revealed in these stabilities was irregular. EDA indicated the more stabilizing back-donative CTPLX $\left(\mathrm{XH}_{3} \rightarrow \mathrm{H}_{2}\right)$ term for X $=\mathrm{Sb}$ than $\mathrm{X}=\mathrm{As}$ as contributing to the irregularity found. ${ }^{33}$ The TSs for $\mathrm{H}_{2}$ elimination from $\mathrm{XH}_{5}\left(D_{3 h}\right)$, optimized at the correlated level, possessed $C_{s}$ symmetry and were equatorialequatorial (eq-eq) for $\mathrm{X}=\mathrm{P}, \mathrm{As}$, and Sb , whereas zwitterionic axial-equatorial (ax-eq) for $\mathrm{X}=\mathrm{Bi}$. We related the different nature of the $\mathrm{H}_{2}$ elimination TS for $\mathrm{X}=\mathrm{Bi}$ to the high exothermicity ( $-73 \mathrm{kcal} / \mathrm{mol}$ ) of the reaction $\mathrm{BiH}_{5}\left(\mathrm{D}_{3 h}\right) \rightarrow$ $\mathrm{BiH}_{3}\left(C_{3 v}\right)+\mathrm{H}_{2}$. As the computed barrier heights to $\mathrm{H}_{2}$ loss
appeared to be at least $30 \mathrm{kcal} / \mathrm{mol}$ above $\mathrm{XH}_{5}\left(D_{3 h}\right)$, all the $\mathrm{XH}_{5}$ species might be kinetically stable. ${ }^{32}$ On the other hand, the isolation of $\mathrm{XH}_{5}$ based on the $\mathrm{XH}_{3}\left(C_{3 v}\right)+\mathrm{H}_{2}$ reaction seems to be unrealistic due to the large barriers to overcome of $\sim 75$, $\sim 85, \sim 85$, and $\sim 105 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{X}=\mathrm{P}, \mathrm{As}, \mathrm{Sb}$, and Bi , respectively ${ }^{28}$ (for $\mathrm{X}=\mathrm{P}$, this was also pointed out before ${ }^{5 e}$ ).

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Supporting Information Available: Tables giving a complete set of total energies obtained from both ECP and AE calculations ( 3 pages). This material is contained in many libraries on microfiche, immediately follows this article in the microfilm version of the journal, can be ordered from the ACS, and can be downloaded from the Internet; see any current masthead page for ordering information and Internet access instructions.

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    (25) For the RHF/ECP equilibrium geometries of the $\mathrm{XH}_{3}$ and $\mathrm{H}_{2}$ molecules see footnote $b$ in Table 3 .
    (26) The increasing charge separation between the central atom $X$ and both kinds of hydrogens in the $D_{3 h}$ and $C_{4 v}$ forms of $\mathrm{XH}_{5}$ on going from X $=\mathrm{P}$ to $\mathrm{X}=\mathrm{As}$ to $\mathrm{X}=\mathrm{Sb}$ is expected on the basis of decreasing electronegativities of X in this direction. Namely, according to Pauling's scale (ref 1 b ) the electronegativity of H is 2.1 and the electronegativities of the central atoms decrease as follows: $\mathrm{P}(2.1)>\mathrm{As}(2.0)>\mathrm{Sb}(1.9)=$ Bi (1.9). The predicted slightly smaller charge separations for the $\mathrm{BiH}_{5}$ species as compared to the $\mathrm{SbH}_{5}$ species may have the origin in the "inert pair" effect for the Bi atom. For a discussion of this effect, see ref 19 ; also see ref 21 .

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    (35) The stability calculations ${ }^{17}$ revealed the negative eigenvalues of the triplet instability matrices (ref 36) for the RHF/ECP ax-eq TSs with $\mathrm{X}=$ $\mathrm{Sb}(-0.005)$ and $\mathrm{X}=\mathrm{Bi}(-0.015)$; the computed values of $\left\langle\mathrm{S}^{2}\right\rangle$ for the resulting singlet UHF/ECP solutions were 0.07 and 0.27 , respectively.
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    (38) When the natural charges were recalculated at the UHF/ECP axeq TSs with $\mathrm{X}=\mathrm{Sb}$ and Bi , and by using the UHF/ECP wave functions, only insignificant changes occurred as compared with the RHF/ECP charges in Figure 5.

[^6]:    ${ }^{a}$ Energies in $\mathrm{kcal} / \mathrm{mol}$ above the energy of $\mathrm{XH}_{5}\left(D_{3 h}\right)$; the barriers refer to the eq-eq transition states unless noted otherwise, ${ }^{b}$ Refers to the ax-eq zwitterionic transition state. ${ }^{\text {c }}$ At the MP2/ECP geometries. ${ }^{d}$ Numbers in parentheses include the zero-point energy (ZPE) correction calculated at the MP2/ECP level. The ZPE values for $\mathrm{XH}_{5}\left(D_{3 h}\right)$ are (kcal/mol), for $\mathrm{PH}_{5}\left(D_{3 h}\right), 27.6$, for $\mathrm{AsH}_{5}\left(D_{3 h}\right), 25.2$, for $\mathrm{SbH}_{5}\left(D_{3 h}\right), 22.3$, and, for $\mathrm{BiH}_{5}\left(D_{3 h}\right), 20.7$. The ZPE values for the $\mathrm{XH}_{5}\left(C_{5}\right)$ saddle points are $(\mathrm{kcal} / \mathrm{mol})$, for $\mathrm{PH}_{5}\left(C_{5}\right), 25.2$, for $\mathrm{AsH}_{5}\left(C_{5}\right), 23.2$, for $\mathrm{SbH}_{5}\left(C_{5}\right)$, 20.4, and, for $\mathrm{BiH}_{5}\left(C_{s}\right), 18.7$. ${ }^{e}$ Refers to the UHF/ECP optimized transition state (see the text).

[^7]:    ${ }^{a}$ See Chart 1. RHF/ECP energies ( $\mathrm{kcal} / \mathrm{mol}$ ) calculated at the RHF/ECP geometries (subscript ax denotes axial). A negative (positive) sign indicates stabilization (destabilization). ${ }^{b}$ Within the optimized geometries (cf. Figure 1 ). ${ }^{c}$ The data after setting the EX term approximately constant (see the text).

